

## **WARNING**

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Family Name					
Given Name/s					
Student Number					
Teaching Period	Semester 2, 2017				

<b>ENG224 – Electrical Machines and Power Systems</b>	<b>DURATION</b>	
	Reading Time:	<b>10 minutes</b>
	Writing Time:	<b>180 minutes</b>
<b>INSTRUCTIONS TO CANDIDATES</b>		
<b>EXAM CONDITIONS</b>		
<p><u>You may begin writing from the commencement of the examination session.</u> The reading time indicated above is provided as a guide only.</p>		
This is a CLOSED BOOK examination		
Any non-programmable calculator is permitted		
No handwritten notes are permitted		
No dictionaries are permitted		
<b>ADDITIONAL AUTHORISED MATERIALS</b>	<b>EXAMINATION MATERIALS TO BE SUPPLIED</b>	
No additional printed material is permitted	1 x 20 Page Book 1 x Scrap Paper	

**THIS EXAMINATION IS PRINTED  
DOUBLE-SIDED.**

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LEFT BLANK.**

**QUESTION 1****(10 marks)**

Answer the following questions in plain English, without using any equations or formulas.

Answers should be brief and to-the-point. (2 marks each)

- Q1.1** In the problems of magnetic circuits, an air gap is very often included. What is the practical significance of this air gap?
- Q1.2** Why is a transformer more efficient than, for example, an induction motor?
- Q1.3** Is the magnetic circuit (rotor and stator) of a dc machine not laminated?
- Q1.4** What is the reason for most transmission system being AC?
- Q1.5** We talk about friction and windage losses in machines. What is this windage loss and how do you measure it?

**QUESTION 2****(10 marks)**

A 20-kVA, 50-Hz, 2000/200-volt distribution transformer has leakage impedance of  $0.42 + j 0.52$  ohms in the high voltage winding and  $0.004 + j 0.005$  ohm in the low voltage winding. At rated voltage and frequency, the shunt branch admittance (note: not impedance) is  $0.002 - j 0.015$  siemens when seen from the low voltage side. Draw the equivalent circuit of the transformer referred to the high voltage side.

**QUESTION 3****(10 marks)**

A 1-MW, three-phase, star connected, 3.3-kV, 24-pole, 50-Hz synchronous motor has a synchronous reactance of 3.24 ohms per phase. The armature resistance may be ignored. This motor is energized from 3.3-kV infinite bus bars. The field excitation is adjusted until unity power factor at rated load is achieved. Compute the maximum power and torque that the motor can deliver with the excitation remaining unchanged.

**QUESTION 4****(5 marks)**

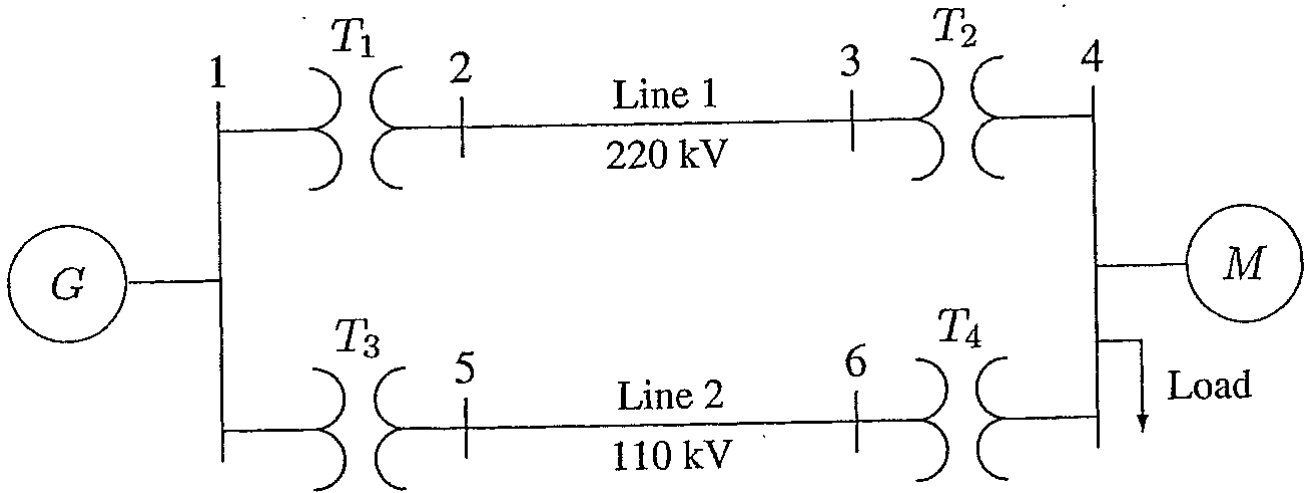
Draw the speed-torque characteristic of a shunt dc motor with torque in the horizontal axis and answer the following questions.

- Q4.1** Does the characteristic indicate a constant-speed machine? Discuss.. (1 mark)
- Q4.2** On the same graph, you wish to draw the characteristic of a differential compound dc motor with the same no-load speed as the separately excited motor. Does this characteristic go above or below the characteristic of the shunt motor? Explain.. (4 marks)

**QUESTION 5**

**(15 marks)**

The one-line diagram of a small three phase power system is shown in Figure 5 below. Load and equipment data are also given in the table following the figure. Determine the component impedances in per unit including the load. Take a common base of 100 MVA and 22 kV at the generator terminals.



**Figure 5** (Ref. Hadi Saadat, Power System Analysis, McGraw Hill,2002.)

System Component	Power rating (MVA)	Voltage rating (kV)	Reactance (%)
Generator, G	90	22	18
Transformer, T <sub>1</sub>	50	22/220	10
Transformer, T <sub>2</sub>	40	220/11	6
Transformer, T <sub>3</sub>	40	22/110	6.4
Transformer, T <sub>4</sub>	40	110/11	8
Motor, M	66.5	10.45	18.5
<b>Line data</b>			
Line 1			48.4 ohms
Line 2			65.43 ohms
<b>Load data</b>			
Load	57	10.45	0.6 pf lagging

**End of questions.**

# FORMULAS

(Symbols have their usual meanings in the context of the particular formula)

**MAGNETIC CIRCUITS:**  $L = \lambda/i = N^2/\mathfrak{R} = \mu N^2 A/d$ ;  $Ni = \sum H\lambda = \phi \mathfrak{R}$ ;  $B = \mu H = \mu Ni/\lambda$ ;  
 $\mu = \mu_r \mu_0$ ;  $\mathfrak{R} = \lambda/\mu A$

**TRANSFORMERS:**  $\frac{V_1}{V_2} = \frac{I_2}{I_1} = \frac{N_1}{N_2}$ ;  $Z_1 = \left(\frac{N_1}{N_2}\right)^2 Z_2$ ;  $R'_c = \frac{V_{oc}}{I_{oc} \cos\theta}$ ;  $X_m = \frac{V_{oc}}{I_{oc} \sin\theta}$ ;  $\cos\theta = \frac{P_{oc}}{V_{oc} I_{oc}}$ ;

$\eta = \frac{V_2' I_2' \cos\theta}{V_2' I_2' \cos\theta + P_c + R'_{eq} (I_2')^2} \times 100\%$   $\eta_{AD} = \frac{\text{Energy output over 24 hours}}{\text{Energy input over 24 hours}} \times 100\%$

Regulation =  $\frac{\text{No load voltage} - \text{Full load voltage}}{\text{Full load voltage}} \times 100$

## INDUCTION MACHINES: (Torque and power are given on a per phase basis)

$n = 120 \frac{f}{p}$ ;  $s = \frac{(n_s - n)}{n_s}$ ;  $f_2 = sf_1$ ;  $E_{ms} = 4.44f N_{ph} \phi_p K_w$

$V_{th} = \frac{X_m}{\sqrt{R_1^2 + (X_1 + X_m)^2}} V_1$ ;  $R_{th} \cong \left(\frac{X_m}{X_1 + X_m}\right)^2 R_1$   $X_{th} \cong X_1$

$P_{mech} = T_{mech} \omega_{mech} = (1-s)P_{air\_gap}$ ; Ideal Efficiency = 1-s;

$T_{mech} = \frac{1}{\omega_s} I_2'^2 \frac{R'_2}{s} = \frac{1}{\omega_s} \frac{V_{th}^2}{(R_{th} + R'_2/s)^2 + (X_{th} + X'_2)^2} \frac{R'_2}{s}$ ;  $P_{air\_gap} = I_2'^2 \frac{R'_2}{s}$

$s_{Tmax} = \frac{R'_2}{\sqrt{R_{th}^2 + (X_{th} + X'_2)^2}}$ ;  $T_{max} = \frac{1}{2\omega_s} \frac{V_{th}^2}{R_{th} + \sqrt{R_{th}^2 + (X_{th} + X'_2)^2}}$

**DC MACHINES:**  $K_a = \frac{Zp}{2\pi a}$ ;  $E_a = K_a \phi \omega$ ;  $T = K_a \phi I_a$ ;  $P_{out} = E_a I_a = T \omega$ ; **La=p wound.**

**ALTERNATORS:**  $E_f \propto I_f$   $E_f = V_t + jI_a X_s$   $E_f = V_t + I_a R_a + jI_d X_d + jI_q X_q$

$P = \frac{|V_t||E_f|}{|Z_s|} \cos(\theta_s - \delta) - \frac{|V_t|^2}{|Z_s|} \cos\theta_s$   $Q = \frac{|V_t||E_f|}{|Z_s|} \sin(\theta_s - \delta) - \frac{|V_t|^2}{|Z_s|} \cos\theta_s$

$E_f = V_t \cos\delta \pm I_d X_d$ ,  $I_a = |I_q| - j|I_d|$  and  $V_t = |V_t|/\underline{-\delta}$

$P = \frac{|V_t||E_f|}{|X_d|} \sin\delta + \frac{|V_t|^2 (X_d - X_q)}{2X_d X_q} \sin 2\delta$   $Q = \frac{|V_t||E_f|}{|X_d|} \cos\delta + |V_t|^2 \left| \frac{\sin^2 \delta}{X_q} + \frac{\cos^2 \delta}{X_d} \right|$

**PER UNIT SYSTEM:**  $Z_{pu} = \frac{Z_{ohm}}{Z_{base}}$ ;  $Z_{base} = \frac{(kV_{base})^2}{MVA_{base}}$ ;

$S_{pu} = kV_{pu} kA_{pu}$  (no  $\sqrt{3}$ );  $kA_{pu} = \frac{MVA_b}{\sqrt{3} kVA_b}$ ;  $Z_{pu2} = Z_{pu1} \times \frac{S_{base2}}{S_{base1}} \times \frac{kV_{base1}^2}{kV_{base2}^2}$

**OTHERS:**  $S = \sqrt{3} V_L I_L$ ; 1 horse power = 746 watts.