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Family Name					
Given Name/s					
Student Number					
Teaching Period	Semester 1, 2018				

ENG432 – Dynamics of Engineering Systems	DURATION	
	Reading Time:	10 minutes
	Writing Time:	180 minutes
INSTRUCTIONS TO CANDIDATES		
<ol style="list-style-type: none"> 1. Read all questions carefully. 2. Answer all questions. 3. Exam is worth 50% of total marks for this unit. 4. Total marks available on this test are 90. 5. Questions are not of equal value. 6. Lecture Textbook permitted: "Mechanical Vibration" by William J. Palm III. 		
EXAM CONDITIONS		
<p><u>You may begin writing from the commencement of the examination session.</u> The reading time indicated above is provided as a guide only.</p>		
This is a RESTRICTED OPEN BOOK examination		
Any non-programmable calculator is permitted		
No handwritten notes are permitted		
No dictionaries are permitted		
ADDITIONAL AUTHORISED MATERIALS	EXAMINATION MATERIALS TO BE SUPPLIED	
Lecture Textbook/s (Unannotated)	1 x 20 Page Book	

**THIS EXAMINATION IS PRINTED
DOUBLE-SIDED.**

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Question 1

A machine of mass $m=1000$ kg is mounted on a simply supported steel beam of length $l=2$ m having rectangular cross section ($h = 0.1$ m, $w = 1.2$ m) and Young's modulus $E=2.06 \times 10^{11}$ N/m². To reduce vertical deflection of the beam, a spring of stiffness k is attached at mid-span (Figure 1). Determine the value of the k to reduce deflection of the beam by

- (a) 25 % of its original value.
- (b) 50 % of its original value.
- (c) 75 % of its original value.

(Marks: 10)

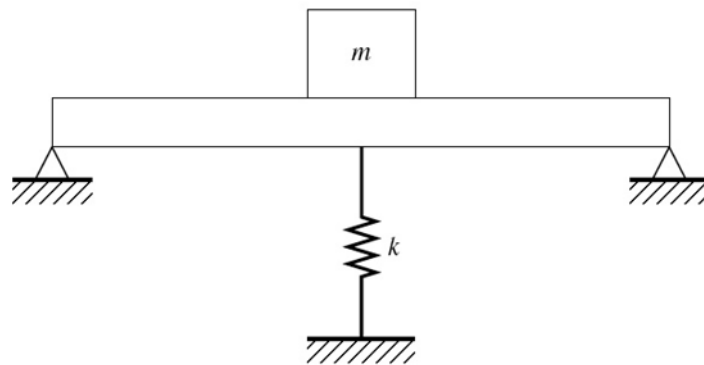


Figure 1*

*W.J.Palm: *Mechanical vibration*, Wiley, 2007, S.S. Rao: *Mechanical vibrations*, Pearson Education, 2011

Question 2

- (a) A spring-mass system has a natural period of 0.21 s. What will be the new period if the spring constant is (i) increased by 50 % and (ii) decreased by 50 %.

(Marks: 6)

- (b) A certain mass-spring system undergoes viscous damping. The mass is 11 kg and the spring constant is 15 000 N/m. The amplitudes in meters of the first through to the fourth cycles of free vibration are 0.098, 0.073, 0.055 and 0.041. Compute the constant c of the system.

(Marks: 9)

Question 3

Find the response of an overdamped single-degree of freedom system subjected to a step force with the equation of motion:

$$2\ddot{x} + 8\dot{x} + 6x = 5u_s(t)$$

Assume the initial conditions as $x_0=1$ and $\dot{x}_0=2$.

(Marks: 20)

Question 4

A mass m is suspended from a spring of stiffness 4000 N/m and is subjected to a harmonic force having amplitude of 100 N and a frequency of 5 Hz. The amplitude of the forced motion of the mass is observed to be 20 mm. Find the value of m (assume undamped case).

(Marks: 15)

Question 5

(a) Find the fundamental frequency for torsional vibration of a shaft of length 2 m and diameter 50 mm when both ends are fixed. The density of the material is 7800 kg/m^3 and the modulus of rigidity is $0.8 \times 10^{11} \text{ N/m}^2$.

(Marks: 5)

(b) A stretched cable of length 2 m has a fundamental frequency of 3000 Hz. Find the frequency of the third mode.

(Marks: 5)

Question 6

Find the free-vibration response of the system shown in Figure 2 for the following set of data: $m_1=2$, $m_2=4$, $k_1=8$, $k_2=4$, $k_3=0$, $c_1=0$, $c_2=0$, $c_3=0$. Assume the initial conditions as $x_1(0)=0$, $x_2(0)=1$, and $\dot{x}_1(0)=0$, $\dot{x}_2(0)=0$.

(Marks: 20)

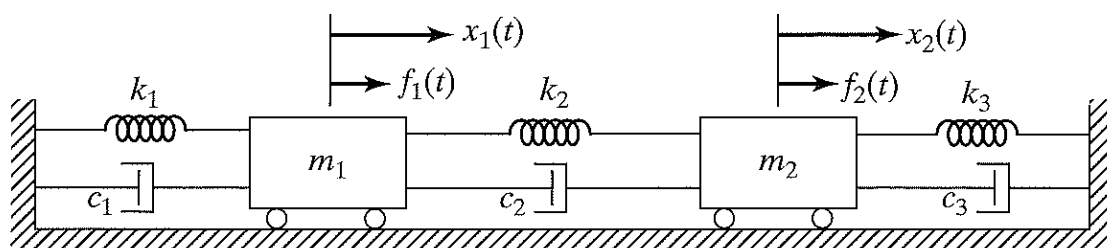


Figure 2*

* S.S. Rao: Mechanical vibrations, Pearson Education, 2011